

| Success Criteria for substitution into a function | | |
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| Instruction | Example | Have you done it? |
| Look at the function | $f(x) = 3x + 4$ | |
| For the rule: $f(-6)$, replace the x with -6 | $f(-6) = 3(-6) + 4$ | |
| Perform the calculation as normal. | $f(-6) = 3(-6) + 4$ $= -18 + 4$ $= -14$ | |

| Success Criteria for Composite Functions | | |
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| Instruction | Example | Have you done it? |
| Find the functions | $f(x) = 2x + 7$ $g(x) = 3x^2$ | |
| Determine which function you do first. In this case, do $f(x)$ and then $g(x)$ | Find $gf(9)$ | |
| Substitute 9 into the function $f(x)$ | $f(9) = 2x + 7$ $= 2(9) + 7$ $= 18 + 7$ $= 25$ | |
| Substitute 25 into $g(x)$ | $g(25) = 3(25^2)$ $= 3(625)$ $= 1875$ | |
| Write out the question and answer | $fg(9) = 1875$ | |

| Success Criteria for Determining the Range or Codomain of a function | | |
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| Instruction | Example | Have you done it? |
| Examine the domain of the function | $f: x \rightarrow 3x + 2$ <i>Domain</i> $1 \leq x < 4$ | |
| Substitute the lowest number into the function | $f(1) = 3(1) + 2 = 5$ | |
| Substitute the next number into the function | $f(2) = 3(2) + 2 = 8$ | |
| Substitute the highest number into the function | $f(4) = 3(4) + 2 = 14$ | |
| State the range or co-domain | $5 \leq f(x) < 14$ | |
| Be careful of excluded values | Check that if you have functions such as $g(x) = \frac{2}{3+x}$ you miss out -3 as this would mean division by zero. | |

| Success Criteria for finding an Inverse Function | | |
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| Instruction | Example | Have I done it? |
| Find the function | $h(x) = \frac{3x + 5}{2}$ | |
| Write the function out as a function machine. | $x \rightarrow \boxed{\times 3} \rightarrow \boxed{+5} \rightarrow \boxed{\div 2} \rightarrow \frac{3x + 5}{2}$ | |
| Reverse the function machine | $\frac{2x - 5}{3} \leftarrow \boxed{\div 3} \leftarrow \boxed{-5} \leftarrow \boxed{\times 2} \leftarrow x$ | |
| Write out the new function | $g^{-1}(x) = \frac{2x - 5}{3}$ | |

| Success Criteria for finding an Inverse Function: the efficient method | | |
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| Instructions | Example | Have I done it? |
| Locate the function | Find the Inverse function of $f(x) = \frac{\sqrt{5x+1}}{4}$ | |
| Let $y = f(x)$ | $y = \frac{\sqrt{5x+1}}{4}$ | |
| Swap round the x and ys | $x = \frac{\sqrt{5y+1}}{4}$ | |
| Rearrange to make y the subject | $4x = \sqrt{5y+1}$ $16x^2 = 5y+1$ $16x^2 - 1 = 5y$ $\frac{16x^2 - 1}{5} = y$ $y = \frac{16x^2 - 1}{5}$ | |
| This is the inverse of $f(x)$ | $f^{-1}(x) = \frac{16x^2 - 1}{5}$ | |